5.7 | Electric Dipoles

Learning Objectives

By the end of this section, you will be able to:

- Describe a permanent dipole
- Describe an induced dipole
- · Define and calculate an electric dipole moment
- · Explain the physical meaning of the dipole moment

Earlier we discussed, and calculated, the electric field of a dipole: two equal and opposite charges that are "close" to each other. (In this context, "close" means that the distance *d* between the two charges is much, much less than the distance of the field point *P*, the location where you are calculating the field.) Let's now consider what happens to a dipole when it is

placed in an external field \vec{E} . We assume that the dipole is a **permanent dipole**; it exists without the field, and does not break apart in the external field.

Rotation of a Dipole due to an Electric Field

For now, we deal with only the simplest case: The external field is uniform in space. Suppose we have the situation depicted in **Figure 5.32**, where we denote the distance between the charges as the vector \vec{d} , pointing from the negative charge to the positive charge. The forces on the two charges are equal and opposite, so there is no net force on the dipole. However, there is a torque:

$$\vec{\tau} = \left(\frac{\vec{\mathbf{d}}}{2} \times \vec{\mathbf{F}}_{+}\right) + \left(-\frac{\vec{\mathbf{d}}}{2} \times \vec{\mathbf{F}}_{-}\right)$$
$$= \left[\left(\frac{\vec{\mathbf{d}}}{2}\right) \times \left(+q \ \vec{\mathbf{E}}\right) + \left(-\frac{\vec{\mathbf{d}}}{2}\right) \times \left(-q \ \vec{\mathbf{E}}_{-}\right)\right]$$
$$= q \ \vec{\mathbf{d}}_{-} \times \vec{\mathbf{E}}_{-}$$



Figure 5.32 A dipole in an external electric field. (a) The net force on the dipole is zero, but the net torque is not. As a result, the dipole rotates, becoming aligned with the external field. (b) The dipole moment is a convenient way to characterize this effect. The \vec{d} points in the same direction as \vec{p} .

The quantity $q \vec{\mathbf{d}}$ (the magnitude of each charge multiplied by the vector distance between them) is a property of the dipole; its value, as you can see, determines the torque that the dipole experiences in the external field. It is useful, therefore, to define this product as the so-called **dipole moment** of the dipole:

$$\vec{\mathbf{p}} \equiv q \ \vec{\mathbf{d}} \ . \tag{5.16}$$

We can therefore write

$$\vec{\tau} = \vec{\mathbf{p}} \times \vec{\mathbf{E}} . \tag{5.17}$$

Recall that a torque changes the angular velocity of an object, the dipole, in this case. In this situation, the effect is to rotate the dipole (that is, align the direction of $\vec{\mathbf{p}}$) so that it is parallel to the direction of the external field.

Induced Dipoles

Neutral atoms are, by definition, electrically neutral; they have equal amounts of positive and negative charge. Furthermore, since they are spherically symmetrical, they do not have a "built-in" dipole moment the way most asymmetrical molecules do. They obtain one, however, when placed in an external electric field, because the external field causes oppositely directed forces on the positive nucleus of the atom versus the negative electrons that surround the nucleus. The result is a new charge distribution of the atom, and therefore, an **induced dipole** moment (**Figure 5.33**).



An important fact here is that, just as for a rotated polar molecule, the result is that the dipole moment ends up aligned parallel to the external electric field. Generally, the magnitude of an induced dipole is much smaller than that of an inherent dipole. For both kinds of dipoles, notice that once the alignment of the dipole (rotated or induced) is complete, the net effect is to decrease the total electric field $\vec{E}_{total} = \vec{E}_{external} + \vec{E}_{dipole}$ in the regions inside the dipole charges (Figure 5.34). By "inside" we mean in between the charges. This effect is crucial for capacitors, as you will see in **Capacitance**.



field of the dipole plus the external field.

Recall that we found the electric field of a dipole in **Equation 5.7**. If we rewrite it in terms of the dipole moment we get:

$$\vec{\mathbf{E}}(z) = \frac{1}{4\pi\varepsilon_0} \frac{\vec{\mathbf{p}}}{z^3}.$$

The form of this field is shown in **Figure 5.34**. Notice that along the plane perpendicular to the axis of the dipole and midway between the charges, the direction of the electric field is opposite that of the dipole and gets weaker the further from the axis one goes. Similarly, on the axis of the dipole (but outside it), the field points in the same direction as the dipole, again getting weaker the further one gets from the charges.